

SECTION – I

2. Write short answers to any EIGHT (8) questions :

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- (i) Write the symmetric property and transitive property of equality of the real numbers.
- (ii) Show that $z\bar{z} = |z|^2 \forall z \in C$
- (iii) Find out real and imaginary parts of $(\sqrt{3}+i)^3$
- (iv) Find the modulus of $1-i\sqrt{3}$
- (v) Construct truth table for $(p \wedge \sim p) \rightarrow q$
- (vi) If a, b are elements of a group G , then show that $(ab)^{-1} = b^{-1}a^{-1}$
- (vii) If $A = \begin{bmatrix} 1 & 2 \\ a & b \end{bmatrix}$ and $A^2 = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$, find the values of a and b .
- (viii) If A and B are square matrices of the same order, then explain why in general $(A-B)^2 \neq A^2 - 2AB + B^2$.
- (ix) Define skew-hermitain matrix.
- (x) Evaluate $\omega^{28} + \omega^{29} + 1$
- (xi) When $x^4 + 2x^3 + kx^2 + 3$ is divided by $x-2$, the remainder is 1. Find the value of k .
- (xii) If α, β are the roots of $x^2 - px - p - c = 0$, prove that $(1+\alpha)(1+\beta) = 1-c$

3. Write short answers to any EIGHT (8) questions :

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- (i) Define partial fractions.
- (ii) If $\frac{7x+25}{(x+3)(x+4)} = \frac{4}{x+3} + \frac{B}{x+4}$, then find B .
- (iii) Find the number of terms in A.P if $a_1 = 3$; $d = 7$ and $a_n = 59$
- (iv) If $\frac{1}{a}, \frac{1}{b}, \frac{1}{c}$ are in G.P., show that common ratio is $\pm \sqrt{\frac{a}{c}}$
- (v) Find the sum of $\frac{9}{4} + \frac{3}{2} + 1 + \frac{2}{3} + \dots \infty$
- (vi) If 5 is H.M. between 2 and b , then find b .
- (vii) Write $\frac{(n+1)(n)(n-1)}{3.2.1}$ in factorial form.
- (viii) Prove that ${}^nP_r = n \cdot {}^{n-1}P_{r-1}$
- (ix) Determine probability of getting 2 heads in two successive tosses of balanced coin.
- (x) Show that $8 \cdot 10^n - 2$ is divisible by 6 for $n = 1$ and $n = 2$
- (xi) Find the 6th term in the expansion of $\left(x^2 - \frac{3}{2x}\right)^{10}$
- (xii) Using binomial theorem, find value of $\sqrt[3]{65}$ correct to three places of decimal.

(Turn Over)

4. Write short answers to any NINE (9) questions :

- (i) Verify $\tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta}$ for $\theta = 45^\circ$
- (ii) Prove the identity $\frac{1 + \cos \theta}{1 - \cos \theta} = (\operatorname{cosec} \theta + \cot \theta)^2$
- (iii) If α, β and γ are the angles of triangle ABC then prove that $\tan(\alpha + \beta) - \tan \gamma = 0$
- (iv) Express as product $\cos 6\theta + \cos 3\theta$
- (v) Prove that $1 + \tan \alpha \tan 2\alpha = \sec 2\alpha$
- (vi) Prove that period of cosine is 2π
- (vii) Find the period of $\operatorname{cosec} 10x$
- (viii) Draw the graph of the function $y = \cos x, x \in \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$
- (ix) Write formula for $\cos \frac{\alpha}{2}$ and $\cos \frac{\gamma}{2}$
- (x) Measure of two sides of a triangle are in the ratio 3 : 2 and angle including these sides is 57° . Find the remaining two angles.
- (xi) Define circum centre.
- (xii) Without using calculator / table, show that $2 \cos^{-1} \frac{4}{5} = \sin^{-1} \frac{24}{25}$
- (xiii) Solve the trigonometric equation $\operatorname{cosec}^2 \theta = \frac{4}{3}$

SECTION - II

Note : Attempt any THREE questions.

5. (a) Show that $\begin{vmatrix} a+\lambda & b & c \\ a & b+\lambda & c \\ a & b & c+\lambda \end{vmatrix} = \lambda^2(a+b+c+\lambda)$ 5
- (b) If the roots of the equation $x^2 - px + q = 0$ differ by unity, prove that $p^2 = 4q + 1$ 5
6. (a) Resolve $\frac{1}{(x-3)^2(x+1)}$ into partial fractions 5
- (b) Find n so that $\frac{a^n + b^n}{a^{n-1} + b^{n-1}}$ may be the A.M. between a and b 5
7. (a) Two dice are thrown. E_1 is the event that the sum of their dots is an odd numbers and E_2 is the event that 1 is the dot on the top of the first die. Show that $P(E_1 \cap E_2) = P(E_1) \cdot P(E_2)$ 5
- (b) If $y = \frac{1}{3} + \frac{1.3}{2!} \left(\frac{1}{3}\right)^2 + \frac{1.3.5}{3!} \left(\frac{1}{3}\right)^3 + \dots$ prove that $y^2 + 2y - 2 = 0$ 5
8. (a) Reduce $\sin^4 \theta$ to an expression involving only function of multiple of θ , raised to the first power. 5
- (b) Prove that $\Delta = r^2 \cot \frac{\alpha}{2} \cot \frac{\beta}{2} \cot \frac{\gamma}{2}$ 5
9. (a) Find the values of all the trigonometric functions of the angle -675° . 5
- (b) Prove that $\sin^{-1} \frac{5}{13} + \sin^{-1} \frac{7}{25} = \cos^{-1} \frac{253}{325}$ 5